\hat{p} r $\sigma \hat{j}e$ c $au^{_{152}}$

Phase 25

Tech Active

Question 1

Simple Familiar **OUESTION 1** Technology Active

The acceleration (m s⁻²) of an object moving with simple harmonic motion is modelled by a = -2.95x, where x is its displacement (m) from the origin.

Determine the period of the motion in seconds.

(A) 1.72

(B) 2.13

(C) 2.95

(D) 3.66

Question 2

QUESTION 8 Simple Familian

Technology Active Given $f(x) = \tan^{-1}(2x)$, determine f'(3).

(A) 0.05

(B) 0.15

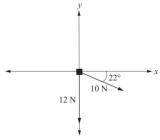
(C) 2.17

(D) 3.10

Question 3

QUESTION 6 Technology Active

Two coplanar forces of magnitudes 12 N and 10 N act on an object in the directions shown. Not to scale



Determine the magnitude of the resultant force acting on the object.

(A) 12.41 N

(B) 15.55 N

(C) 15.69 N

(D) 18.27 N

Question 4

QUESTION 13 (5 marks)

Simple Familiar

An article claims that the mean starting salary of graduates in Australia is currently \$64 800 with a standard deviation of \$4500.

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To check the validity of this claim, an employment agent intends to collect data on the starting salaries of a random sample of 360 graduates.

a) Determine the probability that the sample mean starting salary will be between \$64 000 and \$65 000.

[2 marks]

From the data, the agent calculates a confidence interval for the population mean starting salary of (\$64 589, \$65 811).

b) Determine the sample mean.

c) Comment on the reasonableness of the article's claim based on this confidence interval.

[1 mark] [2 marks]

Ouestion 5

QUESTION 14 (4 marks)

Simple Familiar

At a certain location, a biologist measures the width of a river to be 12 m. She also records the depth of the river at regular 2 m interval widths as shown.

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| Width (m) | 0 | 2 | 4 | 6 | 8 | 10 | 12 |
|-----------|------|------|------|------|------|------|------|
| Depth (m) | 0.52 | 2.15 | 3.70 | 4.27 | 3.32 | 1.28 | 0.59 |

The biologist estimates the cross-sectional area of the river at this location to be 15 m².

Use Simpson's rule to evaluate the reasonableness of this estimation. Justify your area calculation and decision regarding reasonableness using mathematical reasoning.

Question 6

Simple Familia

2023

QUESTION 16 (6 marks)

Complex Familiar Technology Active

Let $\mathbf{A} = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 1 \\ 2 & 2 & 1 \end{bmatrix}$

Given $A^4 = pA^3 + qA^2 + rA + 3I$, use matrix algebra to determine the value of the scalars p, q and r.

Question 7

QUESTION 18 (5 marks)

Complex Unfamiliar

Consider the polynomials $P(z) = z^3 + (i - a)z^2 - 2biz + 3i$ and Q(z) = z - 2i, where $a, b \in R$.

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Given $\frac{P(z)}{Q(z)}$ has a remainder of a-bi, evaluate the reasonableness that (z-(a-bi)) is a factor of P(z).

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