$\hat{p}$ r $\sigma \hat{j}e$ c $au^{_{152}}$ 

## Phase 17

# Tech Free

#### Question 1

#### **OUESTION 7**

The diagram shows a slope field.

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The differential equation represented by the slope field is

(A) 
$$\frac{dy}{dx} = \frac{5y}{x}$$

(B) 
$$\frac{dy}{dx} = \frac{5y^2}{x}$$

(C) 
$$\frac{dy}{dx} = \frac{5y}{x^2}$$

(D) 
$$\frac{dy}{dx} = \frac{5y^2}{x^2}$$

## Question 2

#### **QUESTION 12 (6 marks)**

Given  $z_1 = a + bi$ ,  $z_2 = c + di \ \forall a, b, c, d \in R$ , and  $z_2 \neq 0$ , prove the identity

$$\left| \frac{z_1}{z_2} \right| = \frac{|z_1|}{|z_2|}$$

#### Question 4

## QUESTION 13 (6 marks)

a) Use partial fractions to determine  $\int \frac{22}{(2x-3)(x+4)} dx$ 

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b) Use the result from Question 13a) to determine  $\int_{-3}^{0} \frac{22}{(2x-3)(x+4)} dx$ 

Express your answer in simplest form.

[2 marks]

#### Question 5

#### QUESTION 17 (5 marks)

Complex Familiar

The region between the *x*-axis and the curve of the function  $y = 1 + \sin(2x)$  for  $0 \le x \le \frac{\pi}{2}$  is rotated about the *x*-axis to form a solid of revolution. Technology Free

Determine the volume of this solid. Express your answer in simplest form.